

A Note on Probability

1. The probability of your getting $10\heartsuit$, $J\heartsuit$, $Q\heartsuit$, $K\heartsuit$, and $A\heartsuit$ from a full deck in the first five draws:

$$\frac{5}{52} \times \frac{4}{51} \times \frac{3}{50} \times \frac{2}{49} \times \frac{1}{48} = 3.85 \times 10^{-7}$$

2. The probability of your getting the same cards when there are three players and you have first draw:

$$\begin{aligned} & \frac{5}{52} \times \frac{47}{51} \times \frac{46}{50} \times \frac{4}{49} \times \frac{45}{48} \times \frac{44}{47} \times \frac{3}{46} \times \frac{43}{45} \times \frac{42}{44} \times \frac{2}{43} \times \frac{41}{42} \times \frac{40}{41} \times \frac{1}{40} \\ &= \frac{5}{52} \times \frac{4}{51} \times \frac{3}{50} \times \frac{2}{49} \times \frac{1}{48} = 3.85 \times 10^{-7} \end{aligned}$$

So the number of players doesn't matter.

3. The probability of your getting the same cards when there are three players and you have last draw:

$$\begin{aligned} & \frac{47}{52} \times \frac{46}{51} \times \frac{5}{50} \times \frac{45}{49} \times \frac{44}{48} \times \frac{4}{47} \times \frac{43}{46} \times \frac{42}{45} \times \frac{3}{44} \times \frac{41}{43} \times \frac{40}{42} \times \frac{2}{41} \times \frac{39}{40} \times \frac{38}{39} \times \frac{1}{38} \\ &= \frac{5}{52} \times \frac{4}{51} \times \frac{3}{50} \times \frac{2}{49} \times \frac{1}{48} = 3.85 \times 10^{-7} \end{aligned}$$

So the order of dealing doesn't matter, either.