Announcements – 6 Nov 2014

1. Prayer

2. Exam curve
“Which of the problems from last night's HW assignment would you most like me to discuss in class today?”
Heat

Heat is the transfer of random kinetic energy!

Symbol: \( Q \)

Units: Joules

"Mechanical equivalent of heat": James Joule 1849
calories vs. Calories

1 calorie = 4.186 J

Food calorie: 1 Çal
= a kilocalorie
**“Specific heat”**

How much does $T$ rise when heat energy is added?

- temperature rise is proportional to heat added
- the more mass… the less the temperature rises
- material dependent

$$ Q = mc \Delta T $$

$c =$ “specific heat” (closely related to “heat capacity”)

$m \times c$ sometimes called “thermal mass”

### TABLE 11.1

<table>
<thead>
<tr>
<th>Substance</th>
<th>J/kg·°C</th>
<th>cal/g·°C</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aluminum</td>
<td>900</td>
<td>0.215</td>
</tr>
<tr>
<td>Beryllium</td>
<td>1 820</td>
<td>0.436</td>
</tr>
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<td>Cadmium</td>
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<td>0.055</td>
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<td>Copper</td>
<td>387</td>
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<td>Germanium</td>
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<td>0.077</td>
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<tr>
<td>Glass</td>
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<td>0.200</td>
</tr>
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<td>Gold</td>
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<tr>
<td>Ice</td>
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</tr>
<tr>
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<td>4 186</td>
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Clicker Quiz:
If you add 5 J of heat to a mass of water, and 5 J of heat to the same mass of copper, which one increases the most in temperature?

a. Water
b. Copper

\[ Q = mc \Delta T \]
\[ \Delta T = \frac{Q}{mc} \]

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<td>1.00</td>
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From warmup
The fact that desert sand is very hot in the day and very cold at night is evidence that sand has a:

- a. low specific heat
- b. high specific heat
Phase Changes

From warmup: Thermal energy that is used to melt or freeze something is called:

- a. latent heat
- b. specific heat
- c. thermal mass
Phase Changes

During phase change, no $T$ increase → but heat still needed to complete the phase change → both phases co-exist
Latent Heat Equation

\[ Q = mL \]

\( L \) depends on
- Material
- Type of phase change (i.e. solid-liquid, liquid-gas, or other)

**Water:**

\[
\begin{align*}
L_{\text{melting/freezing}} &= 3.33 \times 10^5 \text{ J/kg} \\
L_{\text{boiling/condensing}} &= 2.26 \times 10^6 \text{ J/kg}
\end{align*}
\]

Caution: these values really depend on pressure (book assumes 1 atm)

**Demo:** boiling water in a vacuum
Clicker quiz

If you want to melt a cube of ice that’s initially at -40°C, which part takes the most energy?

a. Raising the temperature to 0°C
b. Converting from solid to liquid phase
c. Same energy

Water:

\[ c = 4186 \, \text{J/(kg} \, ^\circ\text{C)} \]
\[ L_{\text{melting/freezing}} = 3.33 \times 10^5 \, \text{J/kg} \]

\[
\begin{array}{c}
\text{most} \\
\text{least}
\end{array}
\]

4186 \times (40 - (-40)) vs. \[ 333000 \]
From warmup

Ralph's professor stated "If you add an ice cube to a glass of water, the temperature of the water does not necessarily decrease." That seems bizarre to him, because ice is obviously used to cool down water! Can you help him understand what his professor may have been talking about?

“Think-pair-share”
- Think about it for a bit
- Talk to your neighbor, find out if he/she thinks the same as you
- Be prepared to share your answer with the class if called on

Clicker: I am now ready to share my answer if randomly selected.
  a. Yes

Note: you are allowed to "pass" if you would really not answer.
Calorimetry

Conservation of energy

\[ Q_{\text{gained by cold objects}} = Q_{\text{lost by hot objects}} \]

(assuming no heat flow to outside)

→ On both sides of equation use only \textit{positive} quantities (absolute values)

→ Don’t forget melting and boiling \( mL \) terms if needed

\[ Q_{\text{total}} = 0 \]

My method vs. book’s method

\[ Q_{\text{generated by cold}} + Q_{\text{generated by hot}} = 0 \]
Worked Problem

200 g of iron at 100°C is added to an insulated container with 200 g of ice at -10°C. How much ice melts if they come to equilibrium at 0°C? (Don’t worry about the change in temperature of the container itself.)

Ref: 
\[ c_{\text{iron}} = 448 \text{ J/kg} \cdot \text{°C} \]
\[ c_{\text{water}} = 4186 \text{ J/kg} \cdot \text{°C} \]

Start with: \[ Q_{\text{gained by ice}} = Q_{\text{lost by iron}} \]

\[
(m \cdot c \Delta T)_{\text{iron to 0°C}} + (m \cdot L)_{\text{ice melts}} = (m \cdot c \Delta T)_{\text{iron to 0°C}}
\]

\[
m_{\text{iron}} \Delta T_{\text{iron}} + m_{\text{ice}} \Delta T_{\text{ice}} = m_{\text{iron}} c_{\text{iron}} \Delta T
\]

\[
m_{\text{ice}} \Delta T_{\text{ice}} = m_{\text{iron}} c_{\text{iron}} \Delta T
\]

\[
\text{Answer: } 14.35 \text{ g}
\]
Worked Problem

5 g of hot iron at 300° C is added to 100 g of water at 30° C. What is the final temperature?

\[
Q_{\text{gained by water}} = Q_{\text{lost by iron}}
\]

\[
(mCST)_{\text{water}} = (mCST)_{\text{iron}}
\]

\[
m_{\text{water}} \cdot C_{\text{water}} \cdot (T_f - 30) = m_{\text{iron}} \cdot C_{\text{iron}} \cdot (300 - T_f)
\]

\[
m_{\text{water}} \cdot T_f - m_{\text{water}} \cdot 30 = m_{\text{iron}} \cdot C_{\text{iron}} \cdot 300 - m_{\text{iron}} \cdot C_{\text{iron}} \cdot T_f
\]

\[
m_{\text{water}} \cdot T_f + m_{\text{iron}} \cdot C_{\text{iron}} \cdot T_f = m_{\text{water}} \cdot 30 + m_{\text{iron}} \cdot C_{\text{iron}} \cdot 300
\]

\[
T_f = \frac{m_{\text{water}} \cdot 30 + m_{\text{iron}} \cdot C_{\text{iron}} \cdot 300}{m_{\text{water}} + m_{\text{iron}}}
\]

Answer: 31.44° C
Worked Problem

3000 g of hot iron at 300° C is added to 100 g of water at 30° C. What is the final temperature?

\[ Q_{\text{iron}} = Q_{\text{water}} \]

\[ (mc\Delta T)_{\text{iron}} + mL + (mc\Delta T)_{\text{water}} = (mc\Delta T)_{\text{final}} \]

\[ m_{\text{water}}(100 - 30) + m_w L_v + m_{\text{steam}}(T_f - 100) = m_i C_i (300 - T_f) \]

Solve for \( T_f \)

\[ T_f = 108.7° C \]

Answers: 108.7° C
Worked Problem

500 g of hot iron at 300° C is added to 100 g of water at 30° C. What is the final temperature?

1. Assume none of water turns into steam

\[
(m \cdot c \cdot \Delta T)_{\text{iron}} + m_w \cdot c_w \cdot (T_f - T_w) = m_i \cdot c_i \cdot (300 - T_f)
\]

\[m_w \cdot c_w \cdot (T_f - T_w) = m_i \cdot c_i \cdot (300 - T_f) \quad \rightarrow \quad T_f = 124.1° C
\]

2. Assume all of water turns into steam

\[
(m \cdot c \cdot \Delta T)_{\text{iron}} + m_w \cdot L_v \cdot T_f = (m \cdot c \cdot \Delta T)_{\text{iron}} + (m \cdot c \cdot \Delta T)_{\text{water}}
\]

\[m_w \cdot c_w \cdot (T_f - T_w) + m_w \cdot L_v = m_w \cdot c_w \cdot (T_f - 100) = m_i \cdot c_i \cdot (300 - T_f)
\]

\[\rightarrow T_f = -395.3° C
\]

3. Some of the water

\[
(m \cdot c \cdot \Delta T)_{\text{iron}} + m_{\text{steam}} \cdot L_v = (m \cdot c \cdot \Delta T)_{\text{iron}} + (m \cdot c \cdot \Delta T)_{\text{water}}
\]

\[\rightarrow T_f = 100° C
\]

Answers: 124.1° C (not real answer), -395.3° C (not real answer), 100° C
Question
Why do some things at room temperature feel cold?
Heat Transfer

- Conduction
- Convection
- Radiation
Clicker quiz
You put the end of a rod in a fire and the other end in a tub of water. The rod that would heat the water fastest will be:
\[ \text{a. short and fat} \]
\[ \text{b. long and fat} \]
\[ \text{c. short and thin} \]
\[ \text{d. long and thin} \]
Thermal conduction:
heat transfer through materials

\[ P = \frac{Q}{time} = kA \left( \frac{T_2 - T_1}{L} \right) \]

- \( k \) = Thermal conductivity of the material (look up on table)
- \( L \) = length/thickness of heat flow
- \( A \) = area of heat flow
Some Thermal Conductivities  
(from your textbook)

<table>
<thead>
<tr>
<th>Material</th>
<th>$k$ (J/s·m·°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Copper</td>
<td>397</td>
</tr>
<tr>
<td>Aluminum</td>
<td>238</td>
</tr>
<tr>
<td>Iron</td>
<td>79.5</td>
</tr>
<tr>
<td>Glass</td>
<td>0.84</td>
</tr>
<tr>
<td>Wood</td>
<td>0.10</td>
</tr>
<tr>
<td>Air</td>
<td>0.0234</td>
</tr>
</tbody>
</table>
“R-value” for a material

\[ R = \frac{L}{k} \]

\[ P = \frac{Q}{t} = A \left( \frac{\left( T_2 - T_1 \right)}{R} \right) \]

Some R-values
(from your textbook)

<table>
<thead>
<tr>
<th>Material</th>
<th>( R ) (( \text{ft}^2 \cdot \circ \text{F} \cdot \text{hr/Btu} ))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Brick, 4” thick</td>
<td>4</td>
</tr>
<tr>
<td>Styrofoam, 1” thick</td>
<td>5</td>
</tr>
<tr>
<td>Fiberglass insulation, 3.5” thick</td>
<td>10.9</td>
</tr>
<tr>
<td>Drywall, 0.5” thick</td>
<td>0.45</td>
</tr>
</tbody>
</table>

1 BTU = 1054 J
Worked Problem

You foolishly decide to build the walls of your new house out of solid aluminum, 5 cm thick. As a result, in the wintertime heat leaks out like a sieve. How much money will this cost you each day? The inside temp is 70° F (21.1° C), the average outside temperature is 25° F (-3.9° C). The surface area is 280 m². The gas company charges you $0.89 per “therm” (1.055 × 10⁸ J). Only count heat loss through conduction.

Answer: $24,286. Yikes!