**Announcements – 22 Sep 2009**

1. If you have questions on exam 1:
   a. Look over your own exam.
   b. Look over the exam solutions, see if you can figure out what you got problems wrong.
   c. Only then should you come talk to me (or Tutorial Lab TAs) about things you still don’t understand.

2. **Newton’s 2nd Law Problems:** $\Sigma F = ma$
   a. Inclined planes
   b. Pulleys
   c. Ropes
   d. Friction
   e. Etc

→ Remember N2 is a blueprint for obtaining a useful equation; it’s not really the equation itself.

The “$\Sigma F$” on the left hand side means you have to consider all of the forces from your FBD and include them on the left hand side.

Do not put any forces on the right hand side!

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**Accelerating Reference Frames (from last time)**

**Demo:** Rotating chair, Ball on string

To be able to ascribe accelerations to real forces, you must be observing the motion from a non-accelerating (constant velocity) point of view

Physics lingo: “point of view” = “reference frame”

Amusement Park Ride: Floor drops out. What are the forces on you?

In **accelerating** reference frames, we tend to invent **fictitious** forces.

Another example: Coriolis force

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**Question:** A car rounds a curve while maintaining a constant speed. Is there a net force on the car as it rounds the curve?

- a. No, because its speed is constant.
- b. No, because the normal force is balanced by gravity.
- c. Yes, because it’s changing direction.
- d. Yes, because it’s slowing down.

**Friction:** *kinetic* and *static*

**Question:** Same box, same magnitude of $F$: which box is easier to get moving?

- a. left is easier
- b. right is easier
- c. same

Friction opposes sliding motion!

(Typically that means it opposes motion, period, but there are rare exceptions…we’ll see one later this lecture)
**From warmup:** Ralph noticed that in the equation for the force of static friction, there’s a "less than or equal to" sign, but in the equation for kinetic friction, there is a plain equals sign. He wants to know why they are different. What should I tell him?

**Answer from the class:**

**Static Friction:**

*Grows with sideways force, to a point….*

At slipping pt:

Friction force proportional to Normal force

\[ F_f = \mu N \]

\( \mu = \text{"coefficient of friction"} \)

**Demo:** Friction blocks

**Kinetic “aka Moving” Friction**

**Demo:** static vs. kinetic friction

**Book figure:**

Compare with the forces when you break a rope tied to a wall. What is the tension in the rope?

**Friction, Summary:**

**Static:**

\[ F_f (\text{max}) = \mu_s N \]

**Kinetic:**

\[ F_f = \mu_k N \]

**Warning:** \( N \) is sometimes equal to \( mg \), but not always!

<table>
<thead>
<tr>
<th>Coefficients of Friction*</th>
<th>( \mu_s )</th>
<th>( \mu_k )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Steel on steel</td>
<td>0.74</td>
<td>0.57</td>
</tr>
<tr>
<td>Aluminum on steel</td>
<td>0.61</td>
<td>0.47</td>
</tr>
<tr>
<td>Copper on steel</td>
<td>0.53</td>
<td>0.36</td>
</tr>
<tr>
<td>Rubber on concrete</td>
<td>1.0</td>
<td>0.8</td>
</tr>
<tr>
<td>Wood on wood</td>
<td>0.25–0.5</td>
<td>0.2</td>
</tr>
<tr>
<td>Glass on glass</td>
<td>0.94</td>
<td>0.4</td>
</tr>
<tr>
<td>Waxed wood on wet snow</td>
<td>0.14</td>
<td>0.1</td>
</tr>
<tr>
<td>Waxed wood on dry snow</td>
<td>—</td>
<td>0.04</td>
</tr>
<tr>
<td>Metal on metal (lubricated)</td>
<td>0.15</td>
<td>0.06</td>
</tr>
<tr>
<td>Ice on ice</td>
<td>0.1</td>
<td>0.03</td>
</tr>
<tr>
<td>Teflon on Teflon</td>
<td>0.04</td>
<td>0.04</td>
</tr>
<tr>
<td>Synovial joints in humans</td>
<td>0.01</td>
<td>0.003</td>
</tr>
</tbody>
</table>

*All values are approximate.

**Worked Problem**

Mary pulls a box of books with mass 25 kg to the right with a rope.

\[ \mu_s = 0.5 \quad \mu_k = 0.3 \quad (\text{Use } g = 10 \text{ m/s}^2) \]

a. First she pulls horizontally on the box with a force of 40 N. The box doesn’t move. What is the frictional force of the floor on the box?

b. What minimum force will she have to exert to get it moving?

**Clicker quiz:** If she pulls with force 175 N, what will the acceleration be after it starts moving?

a. 1 m/s²  b. 2 m/s²  c. 4 m/s²  d. 6 m/s²  e. > 6 m/s²

Answers: 40N, 125 N
Dr Colton’s Guide: How to solve all Newton’s 2\textsuperscript{nd} Law Problems

1. Draw free-body diagrams for each object.
   1b. Divide forces into components if necessary.
   1c. Group objects together if it seems convenient.

2. Use the Newton’s 2\textsuperscript{nd} Law “blueprint equation” to get a “real equation” for each object.
   2b. Do this for each direction if necessary.

3. Plug what you know into the equations, and look at what results.
   3b. Don’t forget to plug in the acceleration, if it’s known.

4. Solve the equations for what you’re looking for.
   4b. Sometimes this involves solving simultaneous eqns.

Worked Problem
If Mary pulls the 25 kg box with force 230 N at an angle of 60\degree above the horizontal, what will the acceleration be? (\mu_k = 0.3)

FBD:

\text{N2 for x:} \hspace{1cm} \text{N2 for y:}

Plug what you know into equations:

Solve the equations for what you’re looking for:

\text{Answers: N = 50.8 N, a = 3.99 m/s}^2

Friction on slopes
Clicker quiz: For the same skis and snow, as the slope angle increases, the ski/snow frictional force
   a. increases
   b. decreases
   c. stays the same

\text{Hint: Man with mass } m: \text{ what is his frictional force on a slope? Use N2.}

The tires on a 5000 kg truck have \mu_s = 0.8, \mu_k = 0.6 (tire to road friction)

What is the maximum stopping deceleration?

What is the maximum stopping deceleration if the wheels are locked?

\rightarrow \text{What do anti-lock brakes do?}

\text{Answers: 0.8g \approx 8 \text{ m/s}^2, 0.6g \approx 6 \text{ m/s}^2}
Warmup questions review

You start to push against a refrigerator. It initially does not budge, but then after you push hard enough it starts sliding along the floor. Which is correct?

a. The friction force was smallest just after the refrigerator started to move.
b. The friction force was largest just after the refrigerator started to move.
c. The friction force was largest just before the refrigerator started to move.
d. The friction force was constant the whole time.

A block is sliding down a ramp with constant speed. There is friction between the block and the ramp. The friction force is:

a. smaller than the component of gravity down the ramp
b. larger than the component of gravity down the ramp
c. equal to the component of gravity down the ramp

A small block is "riding" on top of a large block, which is being pulled to the right with a rope. Both blocks accelerate at the same rate to the right. The force of friction acting on the small block is:

a. to the left
b. to the right
c. nonexistent

Demo: adjustable ramp

Demo Problem: a block on a ramp doesn’t slide until the angle is _____° from horizontal. What is \( \mu_s \)?

Demo Problem: Once the block starts to slide at that angle, it takes ______ s to slide down the ______ m of the ramp. What is \( \mu_k \)?)

Worked Problem: You invent a new Olympic sport called pulley ski jumping. If the kinetic coefficient of friction is \( \mu \), what is your acceleration?

“x” direction  “y” direction

Could you figure this out: How far does the jumper travel?