

Physics 451- Fall 2011

Homework #20

Due Thursday, Nov 15, by 7pm

Please place your assignment in the "Physics 451" slot across from N373 ESC.
Help sessions T Th 3 to 6pm N 337 ESC

List of problems (from the textbook):

4.18

4.19

4.21

4.22

Hints:

For problem **4.18**: The point where to start is to calculate the norm (or the norm square) of the vector $L_{\pm} f_l^m$ in order to determine the expression for A_l^m (or its square). By doing so, you will introduce the product $L_{\pm} L_{\mp}$ which you can replace by its expression in terms of L^2 and L_z (using equation 4.112). Use the fact that f_l^m are normalized.

For problem **4.21**, use a test function in order to apply all the successive derivations.

Trigonometric relationships: $\frac{d}{d\theta} \cot \theta = -\csc^2 \theta = -\frac{1}{\sin^2 \theta}$ and $\csc^2 \theta = 1 + \cot^2 \theta$

Useful integral for problem **4.22**

$$\int_0^{\pi} \sin^{2l+1} \theta d\theta = 2 \frac{2 * 4 * 6 \dots (2l)}{1 * 3 * 5 \dots (2l+1)} = 2 \frac{(2^l l!)^2}{(2l+1)!}$$

For question c), remember the integral for angular normalization: $\int_{\theta=0}^{\pi} \int_{\phi=0}^{2\pi} |Y_l^m|^2 \sin \theta d\theta d\phi$